IŞIK UNIVERSITY, MATH 230 FINAL EXAM

~	Q1	$\mathbf{Q2}$	Student ID:	Row No:
	Q3	Q4		
	Last Name:		First Name:	

1. (10 points)

- i. State 4 different types of **discrete random variables** that you learned in this class.
 - 1.
 - 2.
 - 3.
 - 4.
- ii. State 3 different types of **continuous random variables** that you learned in this class.
 - 1.
 - 2.
 - 3.
- iii. State the main difference between discrete and continuous random variables.

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- 2. (12 points)
 - i. How many permutations are there of the word "MATHEMATICS"?

ii. A ternary string is a word consisting of only 0, 1 or 2. (*For example, 0102 is a ternary string of length 4.*) How many ternary strings of length 4 have at least 2 ones?

iii. In how many ways can 5 people be seated to 7 chairs?

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3. (14 points) There is a game which is played with a coin and two different types of dice. The coin is biased and hence the probability of HEADS is 0.4 whereas the probability of TAILS is 0.6. The first dice is a fair **4-faced** dice and the faces are numbered as 1,2,3,4. The second dice is a fair **6-faced** dice and the faces are numbered as 1,2,3,4,5,6.

First of all, the coin is flipped. If the coin shows HEADS then the **4-faced** dice is rolled. If the coin shows TAILS, then the **6-faced** dice is rolled.

i. What is the probability that the rolled dice shows a 3?

ii. If the rolled dice shows a 3, what is the probability that the coin shows HEADS?

- 4. (12 points) During winter season, there is a probability of 0.2 of having a day with decent weather (temperature above 15 degrees). If we consider that the winter season has 90 days,
 - i. what is the exact probability that there will be at most 2 decent days this winter season?

ii. What is the approximate probability that there will be at most 2 decent days this winter season if you use Poisson distribution.

$ \mathbf{Q5} $	Q6	Student ID:	Row No:
$\mathbf{Q7}$	$\mathbf{Q8}$		
Last Name:		First Name:	

5. (16 points) Random variables X and Y have the joint PMF

$$p_{X,Y}(x,y) = \begin{cases} c|x+y| & \text{if } x = -2, 0, 2 \text{ and } y = -1, 0, 1\\ 0 & \text{otherwise.} \end{cases}$$

i. Find c

ii. What is the probability $\mathbb{P}(Y > X)$?

6. (12 points) 4) Given the following joint PDF:

$$f_{X,Y}(x,y) = \begin{cases} k & \text{if } 0 < x < y < 1\\ 0 & \text{otherwise.} \end{cases}$$

i. Find the value of k.

ii. Determine the conditional pdf $f_{X|Y}(x|y)$

iii. Determine the conditional pdf $f_{Y|X}(y|x)$

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- 7. (12 points) The peak temperature T, in degrees Fahrenheit, on a July day in Antarctica is a Gaussian random variable with a variance of 225. With probability 1/2, the temperature T exceeds 10 degrees.
 - i. What is $\mathbb{P}(T > 32)$, the probability the temperature is above freezing?

ii. What is $\mathbb{P}(T < 0)$?

iii. What is $\mathbb{P}(T > 60)$?

8. (12 points) If the PDF of a continuous random variable X is given as

$$f(x) = \begin{cases} (1/2)e^{-x/2} & \text{if } x \ge 0\\ 0 & \text{otherwise.} \end{cases}$$

i. Find the probability $\mathbb{P}(1 \leq X \leq 2)$.

ii. What is its CDF (cumulative distribution function)?