

Co-registration of pointclouds by 3D Least Squares matching

Devrim Akca and Armin Gruen

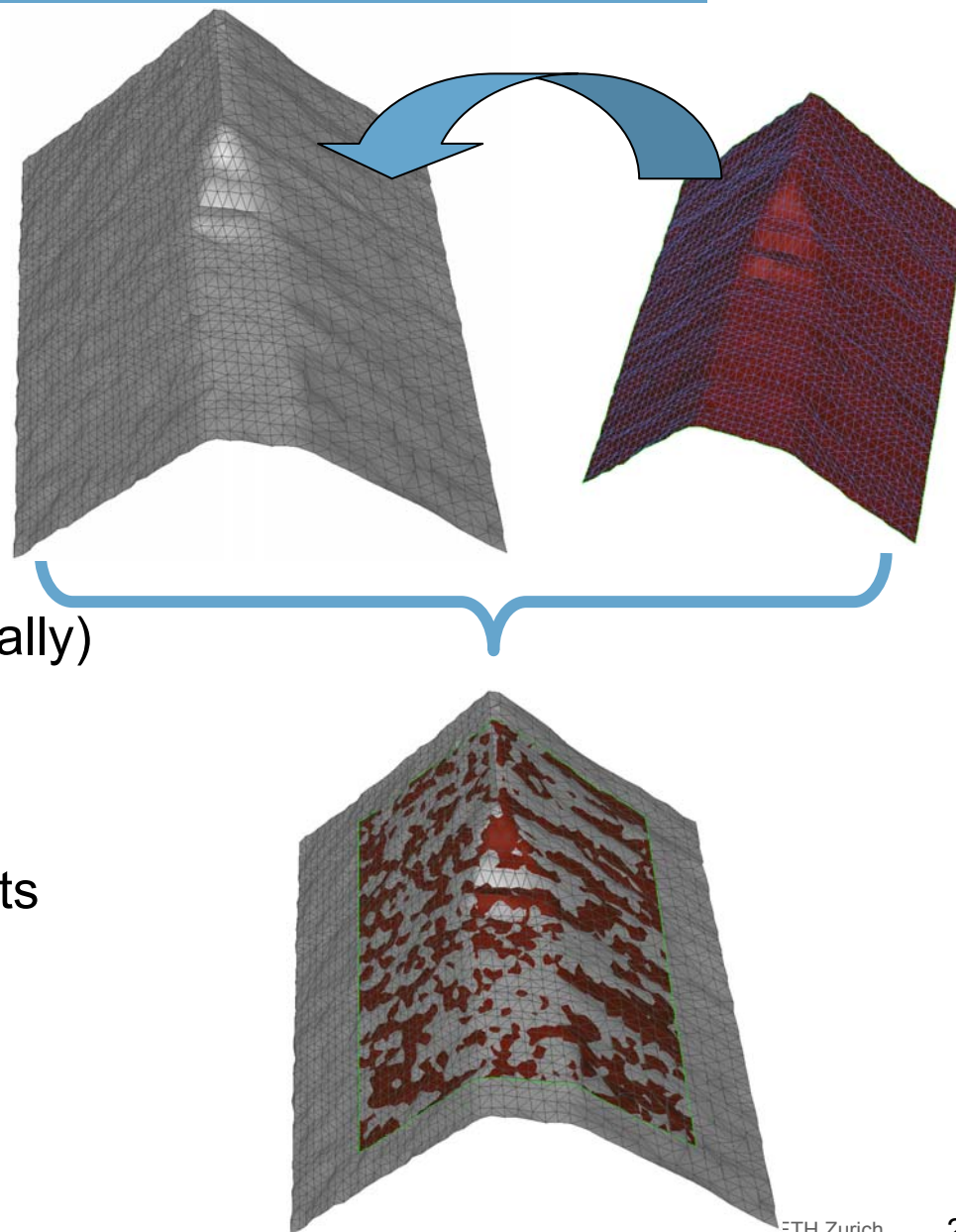
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The Objective: Co-registration of overlapping 3D surfaces

An object surface may be:

- digitized using:
 - + a laser scanner device,
 - + the photogrammetric method,
 - + or other techniques
- acquired:
 - + from different standpoints (spatially)
 - + at different times (temporally)



The goal:

Matching of the conjugate surface parts
and
estimating the 3D transformation

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SIMULTANEOUS MATCHING OF SURFACE GEOMETRY AND INTENSITY

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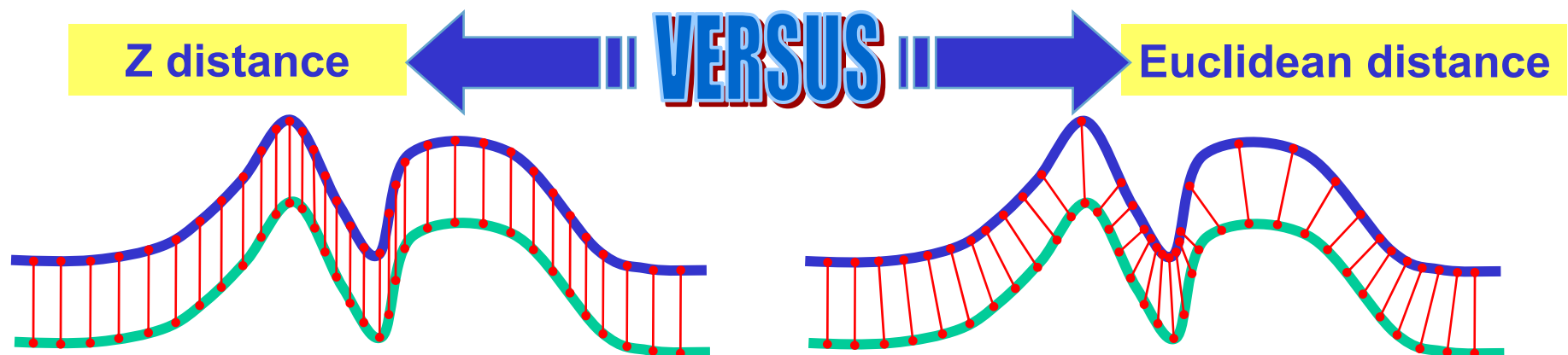
Introduction: Previous work

Least Squares Matching (LSM) (Grün, 1985)

- Surface matching first was addressed as a straight extension of LSM

DEM Matching (Ebner & Müller, 1986; Ebner & Strunz, 1988; Rosenholm & Torlegard, 1988)

- Minimizes height differences along Z-axis by LSs (corresponds to LSM)
- It has been used for:
 - + absolute orientation of stereo models
 - + block triangulation
 - + registration of airborne laser scanner strips



- Valid for **2.5D** surfaces, cannot work with **3D** surfaces

Introduction: Previous work and Motivation

Iterative Closest Point (ICP) (Besl & McKay, 1992; Chen & Medioni, 1992; Zhang, 1994)

- Iterative solution based on closed-form LS rigid transformation
- Converges slowly
- Lacks of internal quality indicators

Motivation: to develop such a surface matcher,

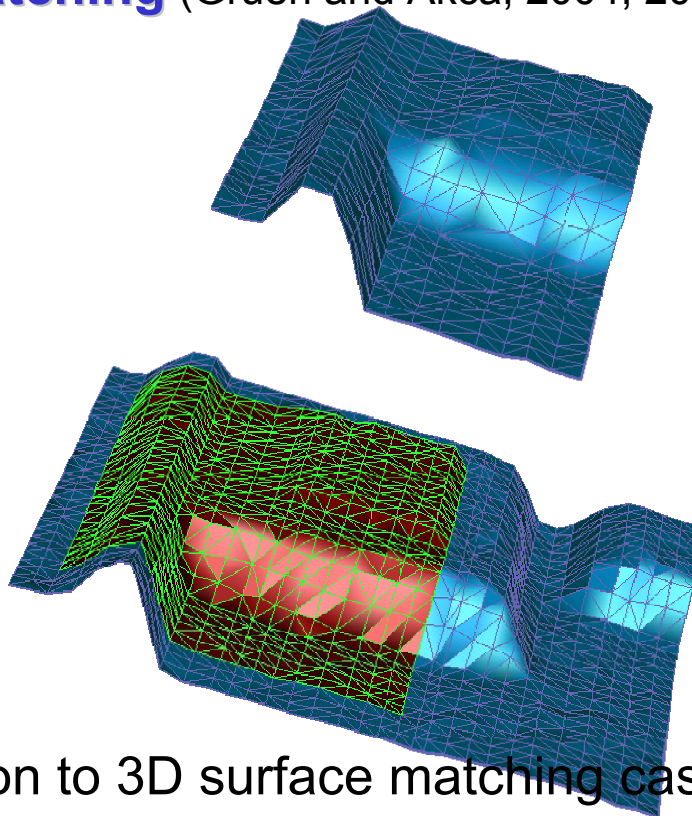
- Matching of fully 3D surfaces (as opposed to 2.5D)
- Rigorous mathematical model for high accuracy demands
- Flexible mathematical model for further algorithmic extensions
- Mechanisms and statistical tools for internal quality control
- Capability of matching of data sets in different quality and resolution

Introduction: Our proposed method LS3D

LS Image Matching (Grün, 1984; 1985)

LS Cuboid (Voxel) Matching (Maas, 1994; Maas and Grün, 1995)

LS 3D Surface Matching (Gruen and Akca, 2004; 2005)



Generalization to 3D surface matching case

The basic estimation model: Observation equations

Two partial surfaces of an object:

- **template surface** $f(x,y,z)$ and **search surface** $g(x,y,z)$ (to be transformed)
- surface representation in a piecewise form
- $f(x,y,z)$ and $g(x,y,z)$ any surface element

3D transformation of the **search surface** $g(x,y,z)$ to be estimated.

In a ideal case,

$$f(x,y,z) = g(x,y,z) \tag{1}$$

Considering the stochastic discrepancies,

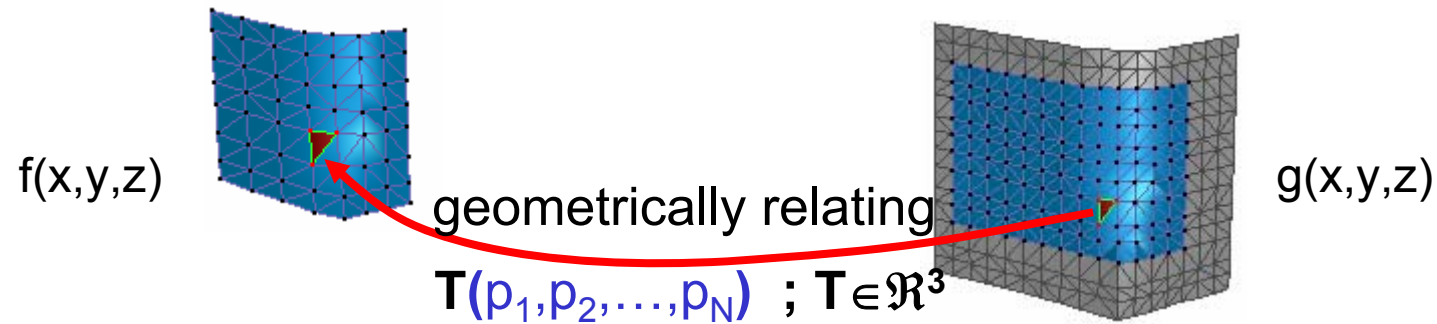
$$f(x,y,z) - e(x,y,z) = g(x,y,z) \tag{2}$$

Equation (2) is **observation equations**

The goal function: $[d_E d_E] = \min$

The final location of $g(x,y,z)$ is estimated w.r.t. an initial position $g^0(x,y,z)$

The basic estimation model: Geometric relationship



Geometric relationship: 7-parameter 3D similarity transformation

$$x = t_x + m(r_{11}x_0 + r_{12}y_0 + r_{13}z_0)$$

$$y = t_y + m(r_{21}x_0 + r_{22}y_0 + r_{23}z_0)$$

$$z = t_z + m(r_{31}x_0 + r_{32}y_0 + r_{33}z_0)$$

(3)

The basic estimation model: Functional model

Non-linear functional model,
 $f(x, y, z) - e(x, y, z) = g(x, y, z)$

(2)

Numerical derivatives

Linearization by Taylor Expansion,

$$f(x, y, z) - e(x, y, z) = g^0(x, y, z) + \frac{\partial g^0(x, y, z)}{\partial x} dx + \frac{\partial g^0(x, y, z)}{\partial y} dy + \frac{\partial g^0(x, y, z)}{\partial z} dz \quad (4)$$

Initial state (approximations)

$$dx = dt_x + a_{10} dm + a_{11} d\omega + a_{12} d\varphi + a_{13} d\kappa$$

$$dy = dt_y + a_{20} dm + a_{21} d\omega + a_{22} d\varphi + a_{23} d\kappa$$

$$dz = dt_z + a_{30} dm + a_{31} d\omega + a_{32} d\varphi + a_{33} d\kappa$$

Differentiation terms

The basic estimation model: Functional model

Final functional model in linearized form:

$$\begin{aligned}
 -e(x, y, z) = & g_x dt_x + g_y dt_y + g_z dt_z \\
 & + (g_x a_{10} + g_y a_{20} + g_z a_{30}) dm \\
 & + (g_x a_{11} + g_y a_{21} + g_z a_{31}) d\omega \\
 & + (g_x a_{12} + g_y a_{22} + g_z a_{32}) d\varphi \\
 & + (g_x a_{13} + g_y a_{23} + g_z a_{33}) d\kappa \\
 & - (f(x, y, z) - g^0(x, y, z))
 \end{aligned}$$

(5)

The functional model in matrix notation:

$$-e = \mathbf{A} \mathbf{x} - \ell, \quad \mathbf{P}$$

weight matrix
design matrix
parameter vector
discrepancies vector

\mathbf{P}

\mathbf{A}

$\mathbf{x}^T = [dt_x \ dt_y \ dt_z \ dm \ d\omega \ d\varphi \ d\kappa]$

$\ell = f(x, y, z) - g^0(x, y, z)$

(6)

The unknown parameters as **stochastic quantities**,

$$-e_b = \mathbf{I} \mathbf{x} - \ell_b, \quad \mathbf{P}_b$$

(7)

The basic estimation model: Mathematical model

The total system is a **Generalized Gauss-Markoff** model:

$$-\mathbf{e} = \mathbf{A} \mathbf{x} - \ell \quad , \quad \mathbf{P} \quad (8)$$

$$-\mathbf{e}_b = \mathbf{I} \mathbf{x} - \ell_b \quad , \quad \mathbf{P}_b \quad (9)$$

The Least Squares solution of the joint system gives as:

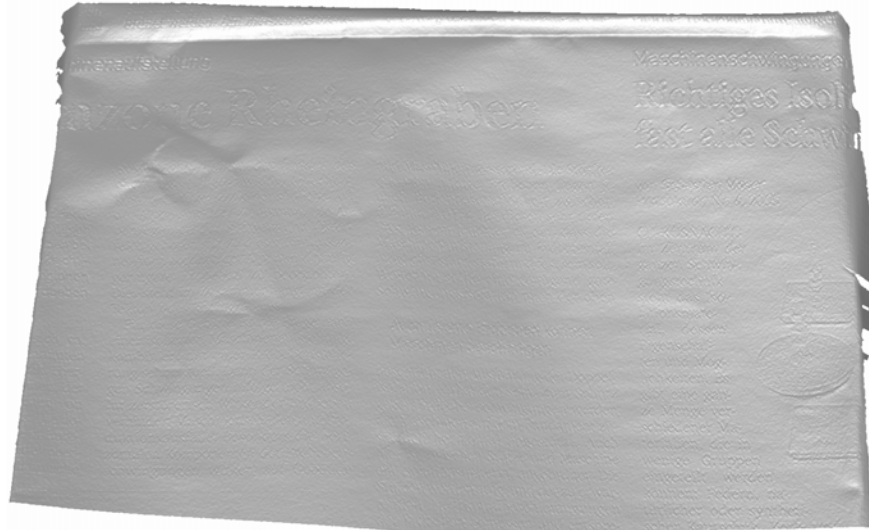
$$\text{Solution vector: } \hat{\mathbf{x}} = (\mathbf{A}^T \mathbf{P} \mathbf{A} + \mathbf{P}_b)^{-1} (\mathbf{A}^T \mathbf{P} \ell + \mathbf{P}_b \ell_b) \quad (10)$$

$$\text{Variance factor: } \hat{\sigma}_0^2 = \frac{\mathbf{v}^T \mathbf{P} \mathbf{v} + \mathbf{v}_b^T \mathbf{P}_b \mathbf{v}_b}{r} \quad (11)$$

The solution is iterative.



Experimental results 1: Newspaper



- **object:** a newspaper
- **scanner:** stereoSCAN^{3D} (Breuckmann)
- **average point spacing:** ~150microns.



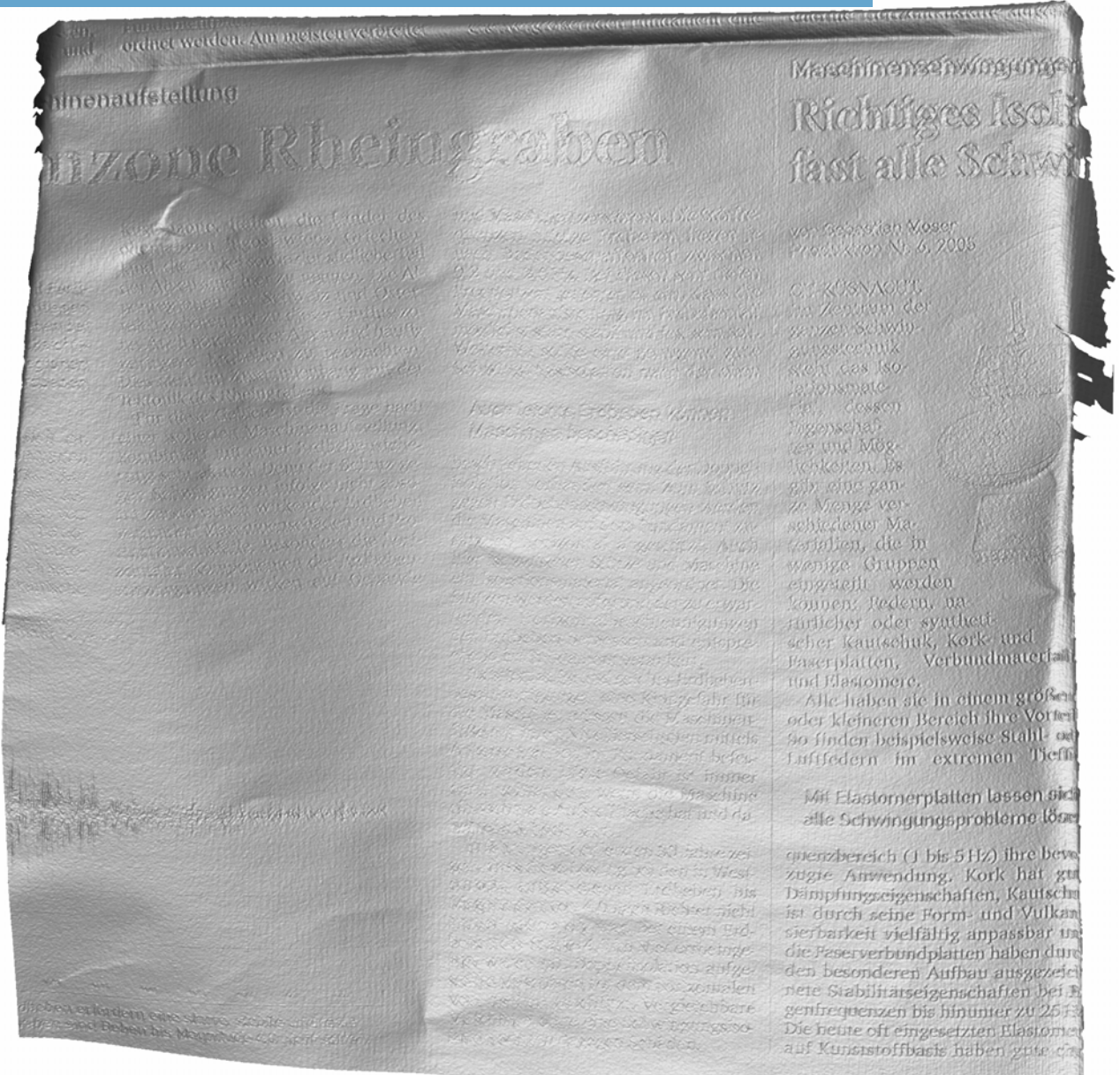
This example:

- Difficult case due to little surface information
- Little changes in surface curvature, almost a plane

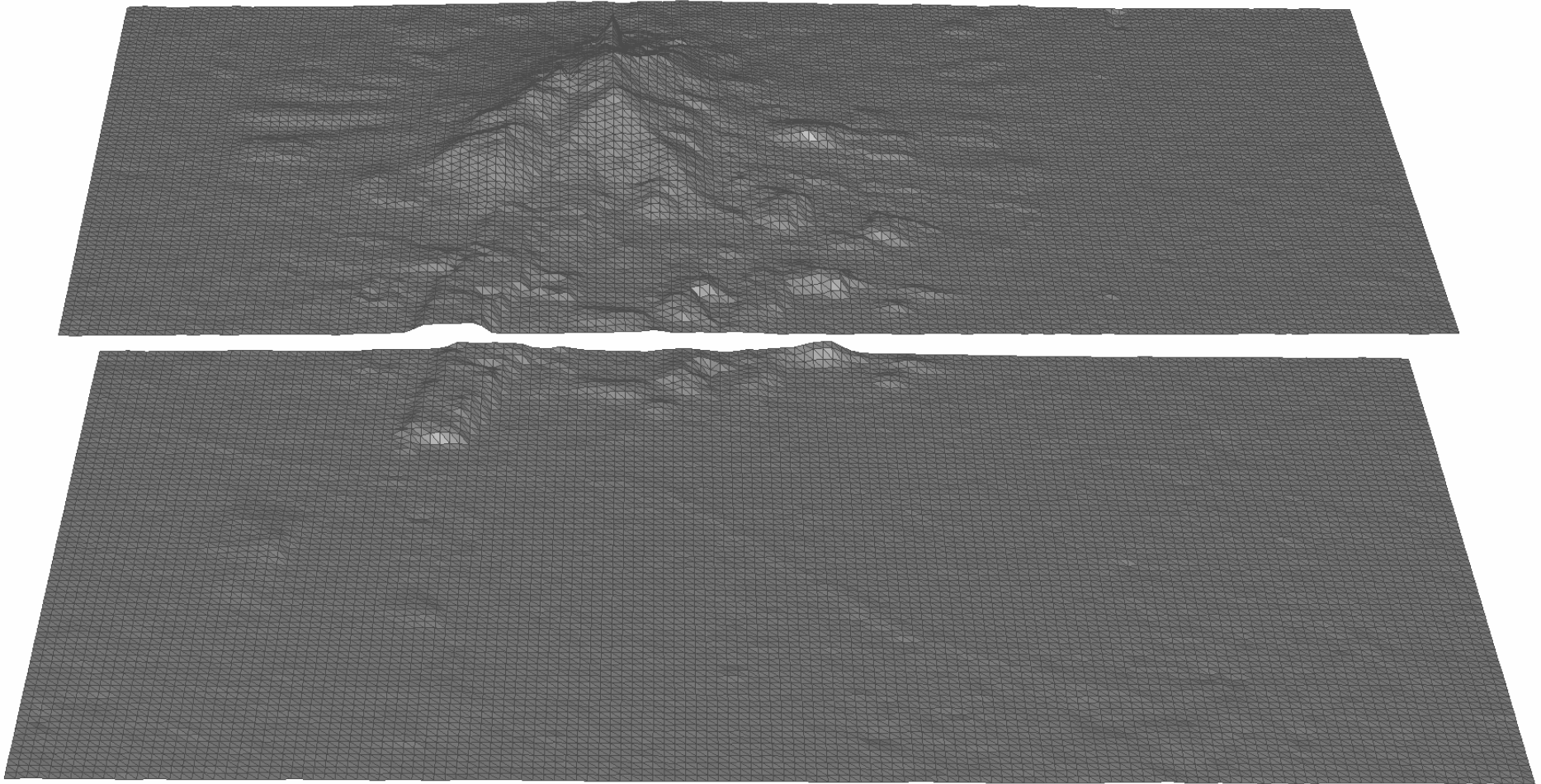
Experimental results 1: Newspaper

The result of the LS3D is successful.

No. points	377K
No. iterations	13
Sigma naught	11.3 μm
Time	36.7 sec.



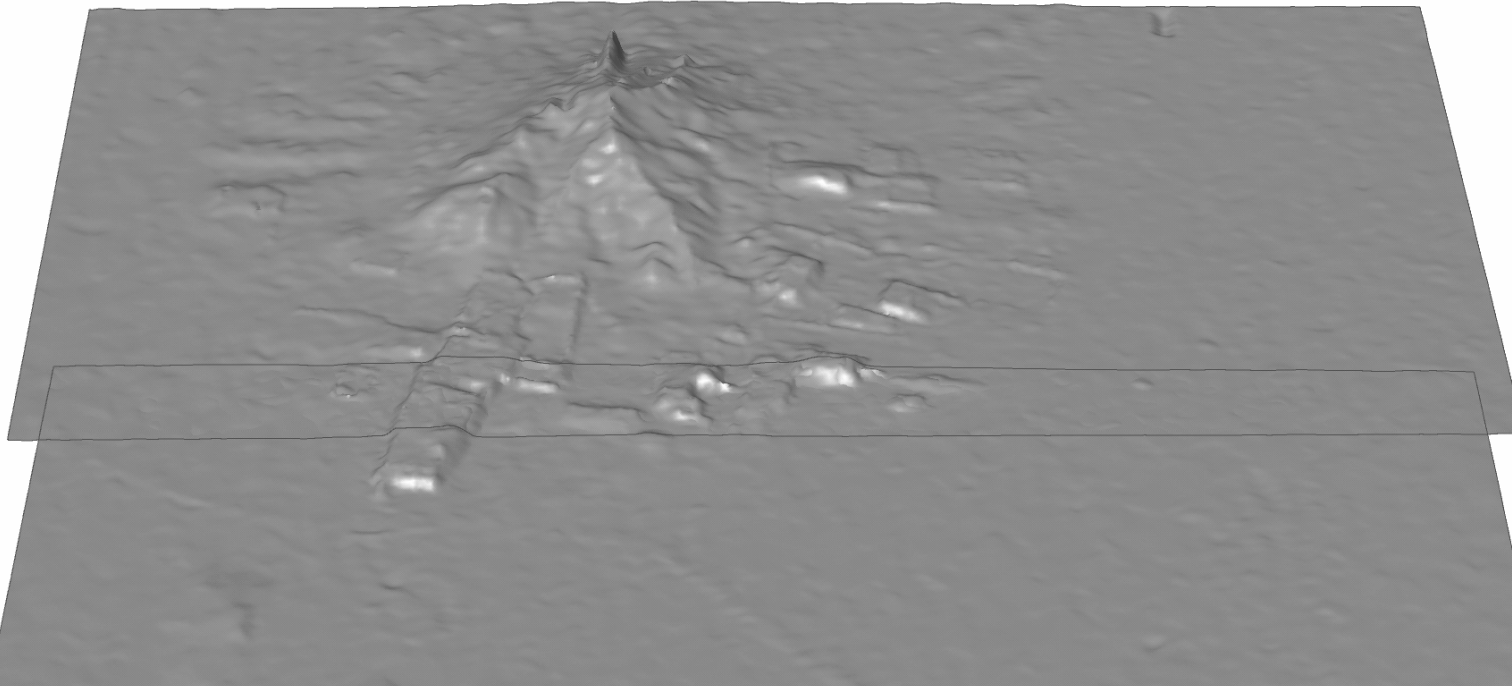
Experimental results 2: Tucume



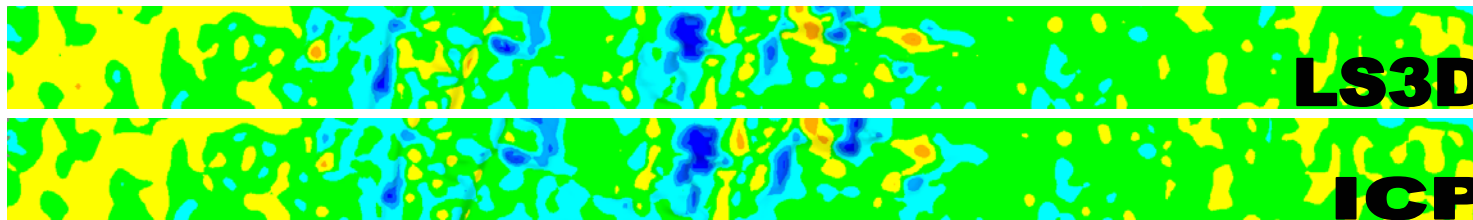
- Two **photogrammetrically** derived DTMs of an area in Tucume (Peru),
- Horizontal resolution is 5 meters,
- **This example:** Difficult case due to very narrow overlap along Y-direction

Data set is courtesy of Martin Sauerbier (ETH Zurich)

Experimental results 2: Tucume



No. of points	Iter.	Sigma (m)	Std.Dev. tx-ty-tz (m)	Std.Dev. ω - ϕ - κ (cc)
12,660	15	1.38	0.16 / 2.74 / 0.20	1.83 / 0.29 / 2.11

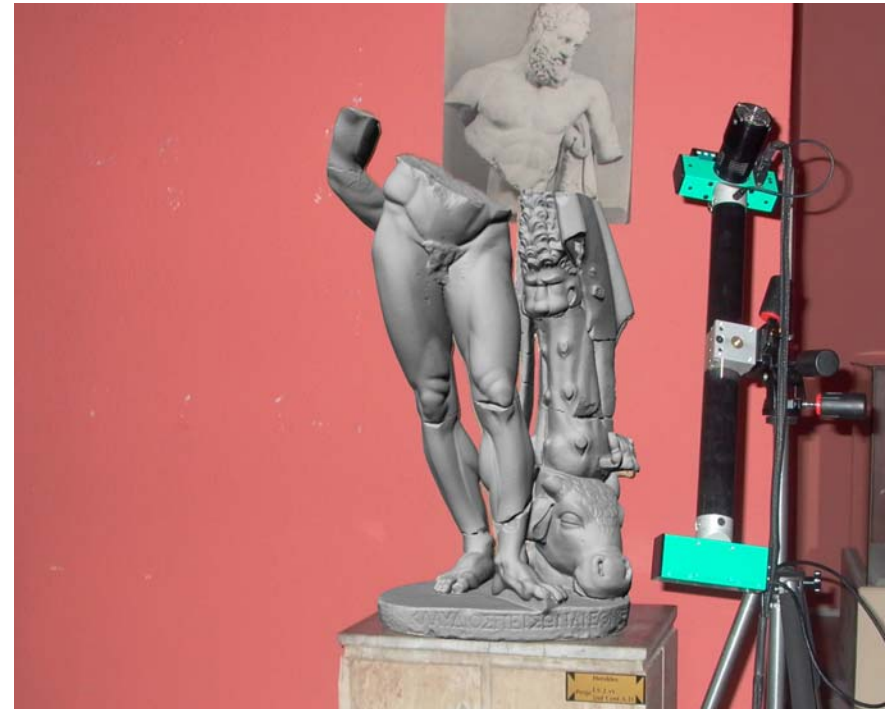


(1.34 m)

Geomagic Studio
(1.42 m)



Experimental results 3: Weary Herakles



- Cultural heritage application
- 3D modeling of the lower part of a marble Herakles statue
- In the Antalya Museum

This example shows:

- Co-registration of multiple surfaces

Experimental results 3: Weary Herakles

- Digitization in the Antalya Museum
- Breuckmann optoTOP-HE coded structured light system
- 1 ½ days on site work with 67 scans
- 83.75M points in total



Devrim Akca, ILMF'08, Denver (CO), February 21, 2008.

Experimental results 3: Weary Herakles

234 consecutive pairwise LS3D matching. The average sigma naught is **81 microns**.

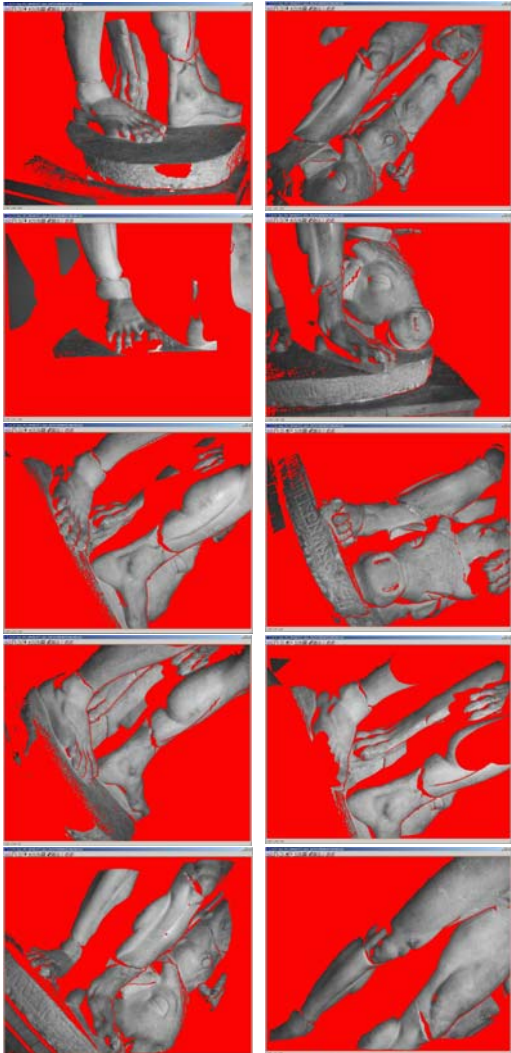


Example: Registration of 1st and 2nd scans
Note: 3x3 down-sampling for better visualization



Experimental results 3: Weary Herakles

Global registration with the block adjustment by independent models solution
Sigma naught **47 microns**, in agreement with the system specifications



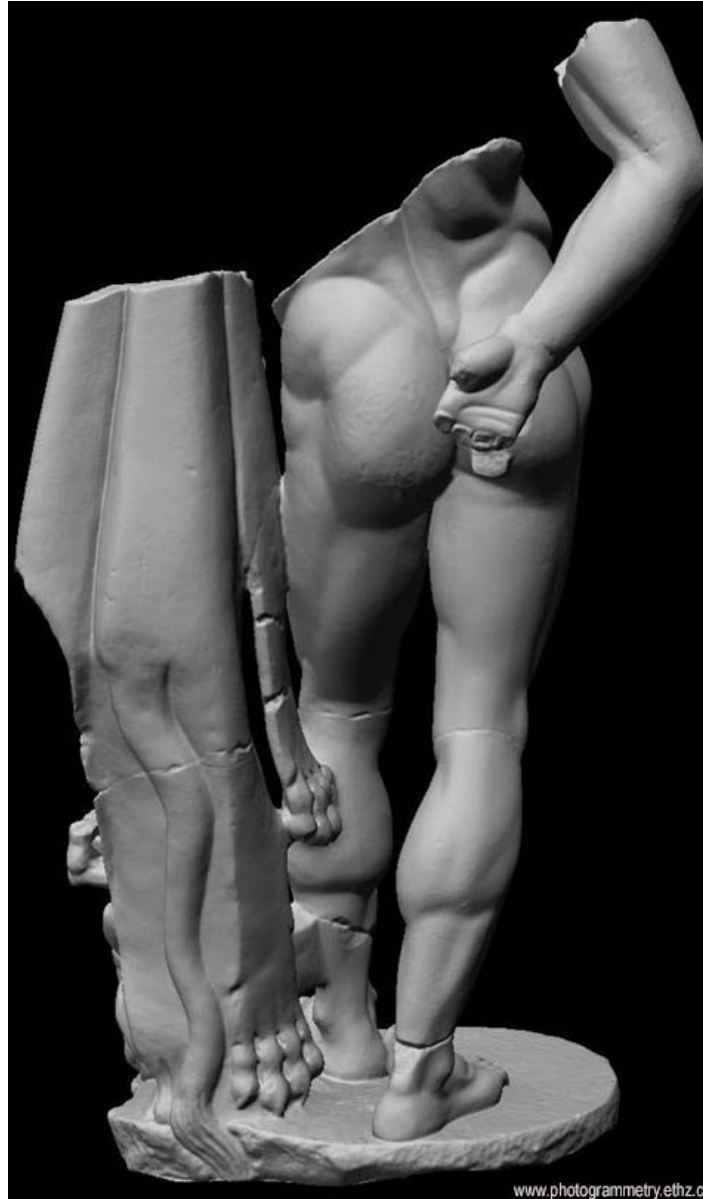
Example: Registration of first 10 scans
Note: 3x3 down-sampling for better visualization



Experimental results 3: Weary Herakles

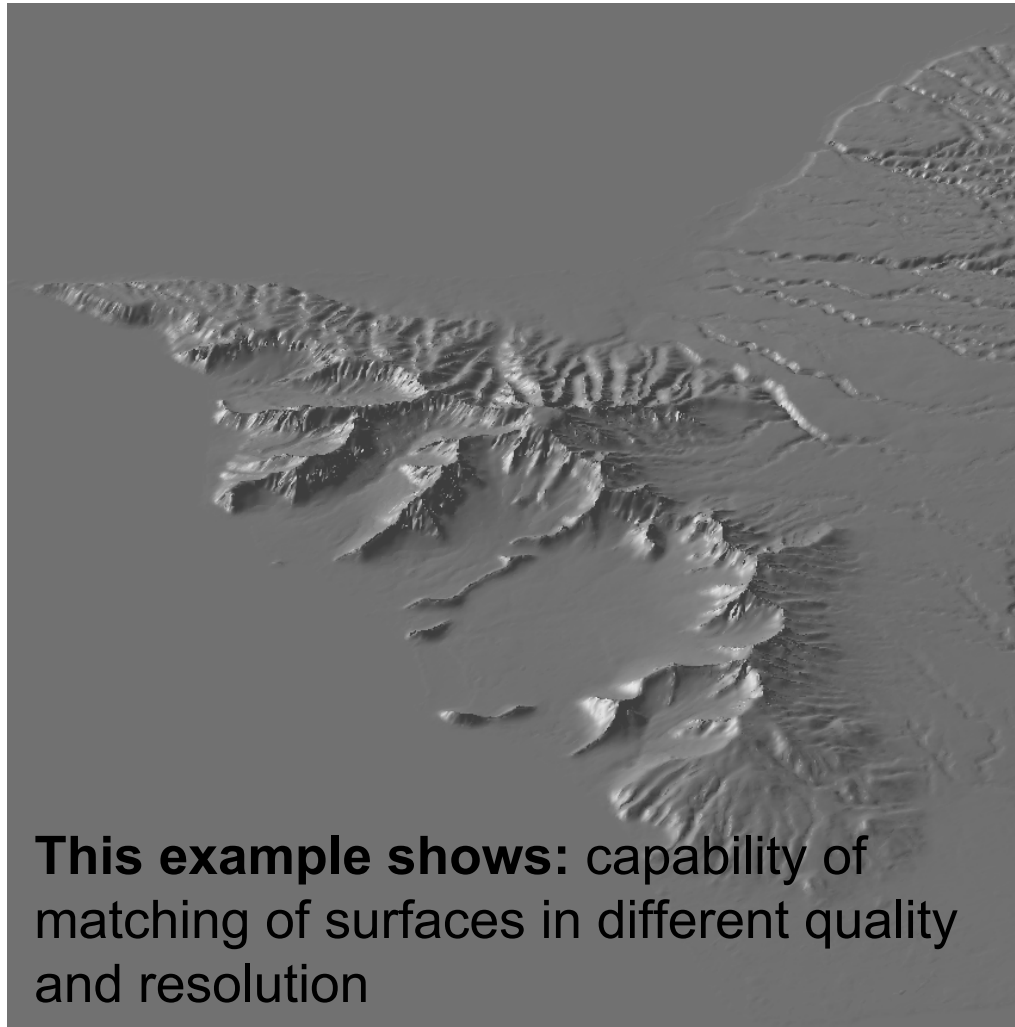


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Experimental results 4: Filling the data holes of SRTM C- DEMs



This example shows: capability of matching of surfaces in different quality and resolution



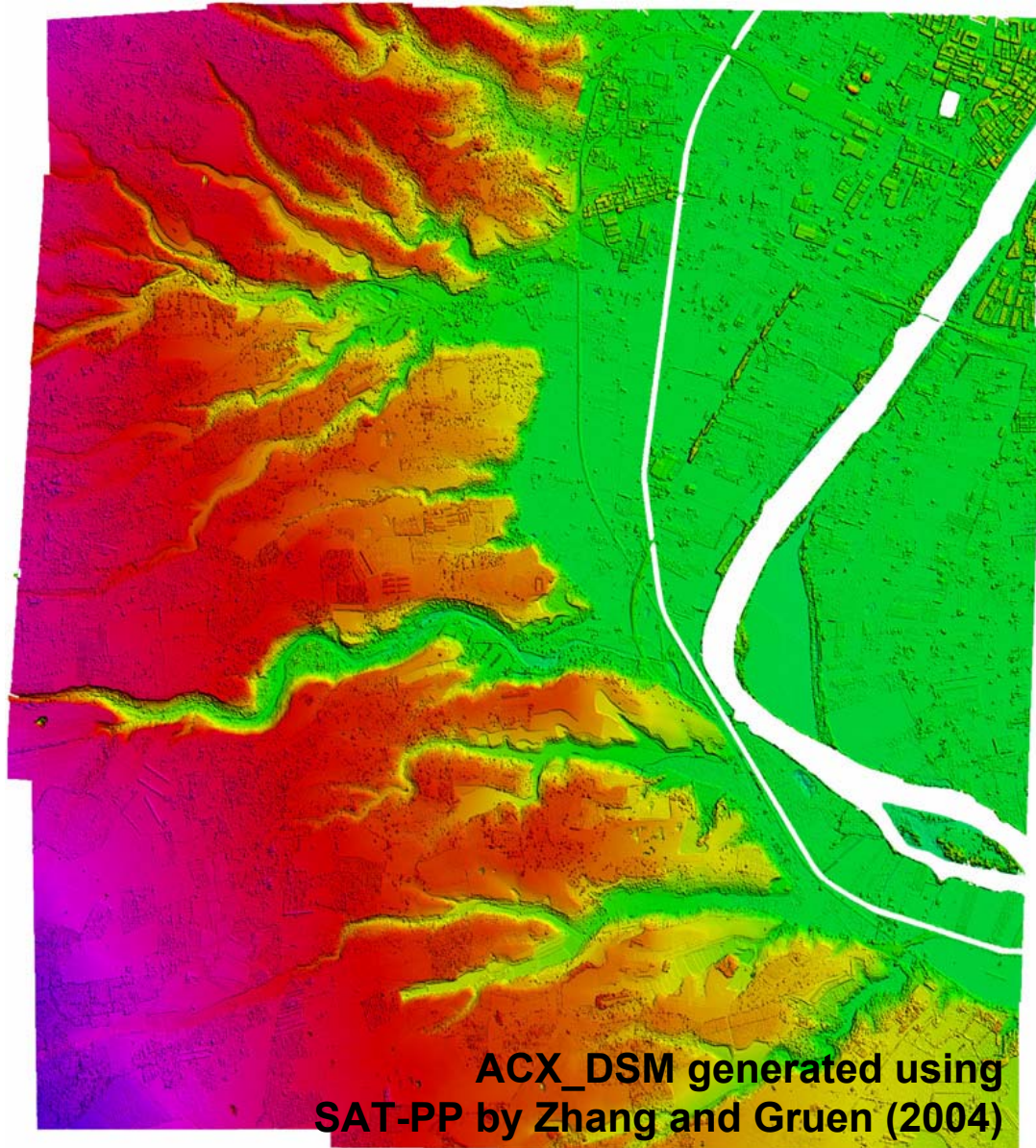
Devrim Akca, ILMF'08, Denver (CO), February 21, 2008.

A cooperative project:



- Jeppesen: a worldwide terrain database for aviation
- Swissphoto: DB generation
- SRTM C-Band DEMs basedata,
- Data holes due to typical problems of InSAR,
- Filling the dataholes by local DEMs in **any available quality/resolution**,
- Correction of the reference frame differences (translation and rotation) by the LS3D
- SRTM TerrainScape™

Experimental results 5: Accuracy evaluation of DMC's DSMs



Task: Quality evaluation of the DSMs derived by **DMC digital airborne camera** imagery

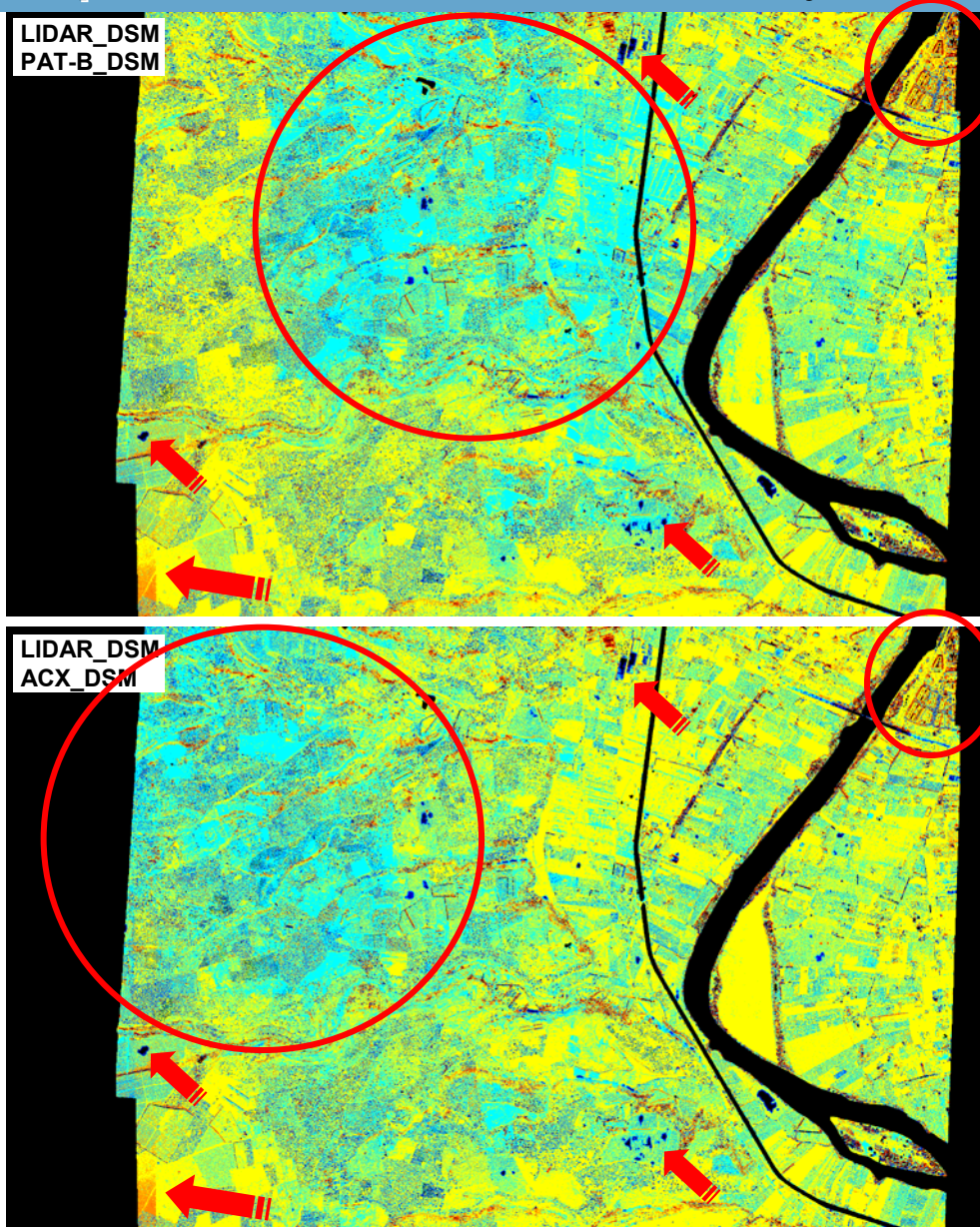
DMC DSMs

- 28 images in 4 parallel strips
- PAT-B -> SAT-PP -> DSM (1m)
- ACX -> SAT-PP -> DSM (1m)

LIDAR DSM (reference)

- Simultaneous acquisition with DMC
- Optech 3030
- 1.2 pnt/m2, interpolated to 2m grid spacing

Experimental results 5: Accuracy evaluation of DMC's DSMs



Residuals of the Euclidean distances after the LS3D matchings,

LIDAR DSM: template
DMC DSMs: search

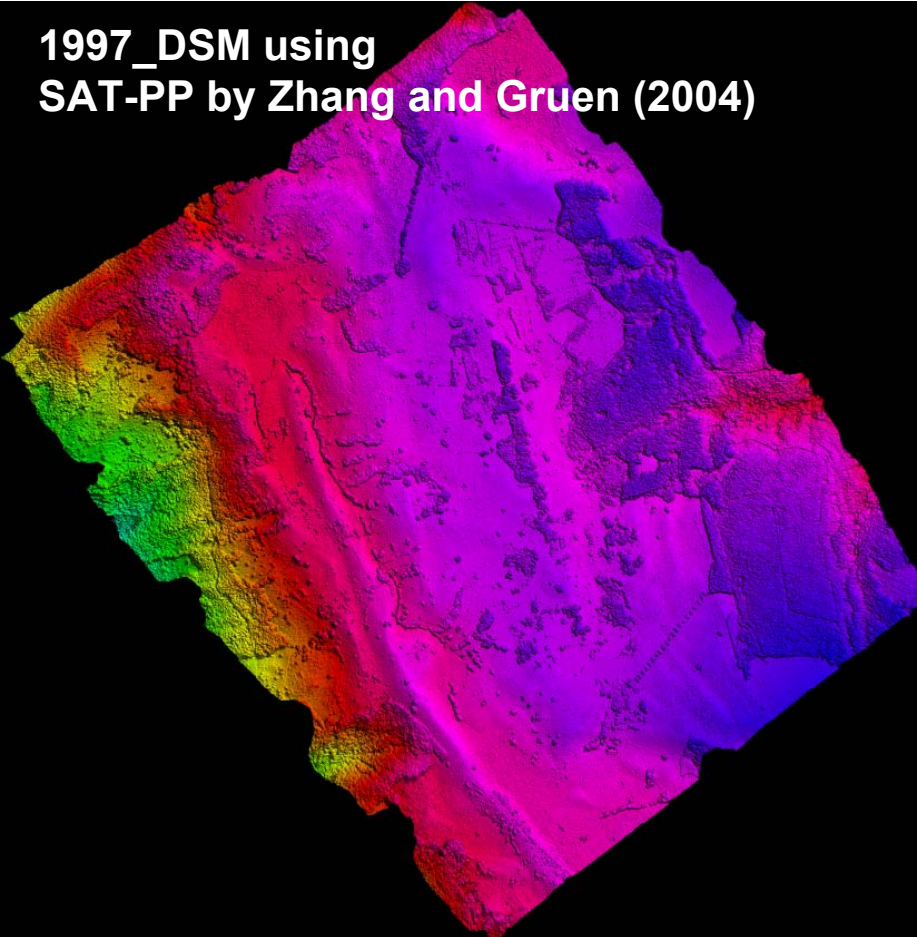
Residuals reveal many problems:

- PAT-P and ACX orientations are apparently different
- Large differences at discontinuities, at top-right, urban area
- A systematic effect at lower left, orange jump. Most possibly due to image matcher.
- Occasional errors of the image matcher

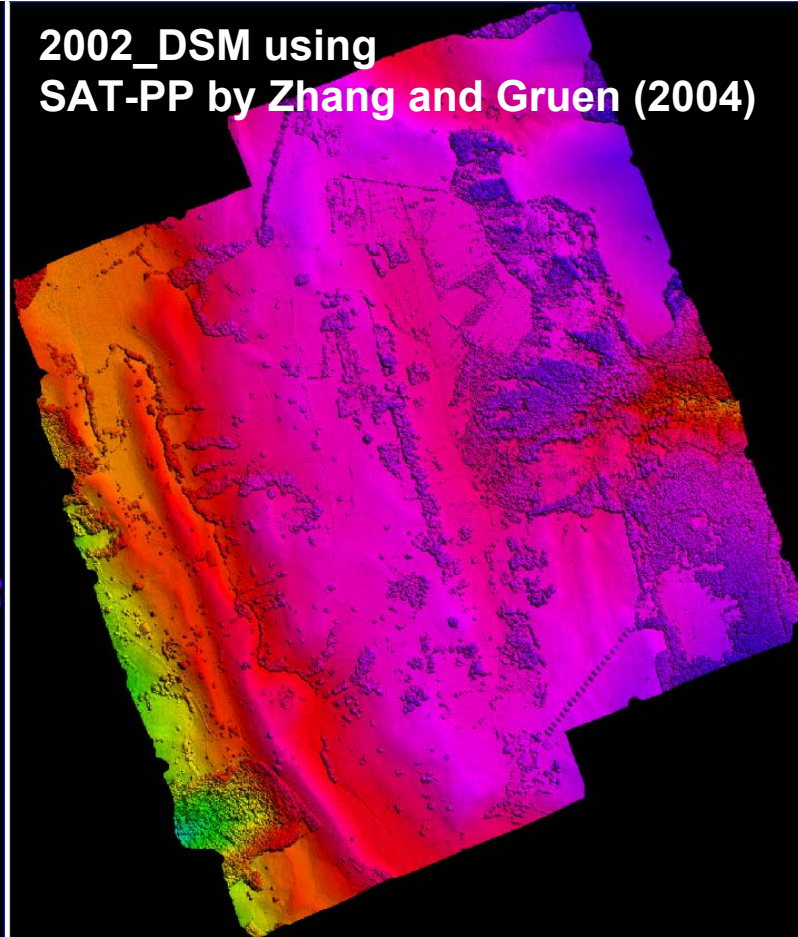


Experimental results 6: Change detection, deforestation analysis

**1997_DSM using
SAT-PP by Zhang and Gruen (2004)**



**2002_DSM using
SAT-PP by Zhang and Gruen (2004)**



Task: Analysis of change detection and deforestation

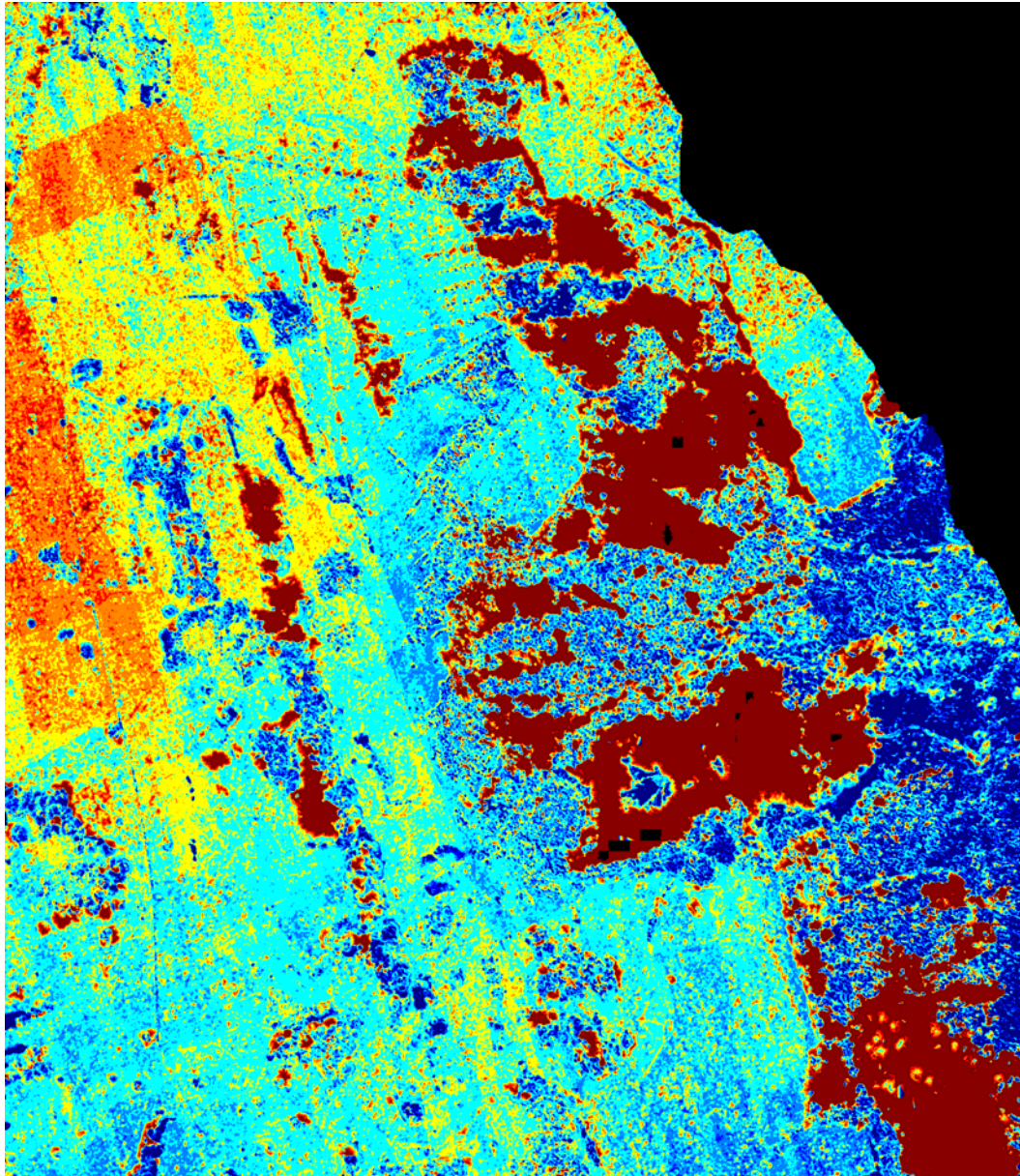
1997_DSM and 2002_DSM

- RC30 analog camera
- 0.5m grid spacing

2001_LIDAR_DSM

- Swisstopo
- 1-2pnt/m² -> 2.5m grid spacing

Experimental results 6: Change detection, deforestation analysis



Z-components of the residuals of the Euclidean distances after the LS3D matching of

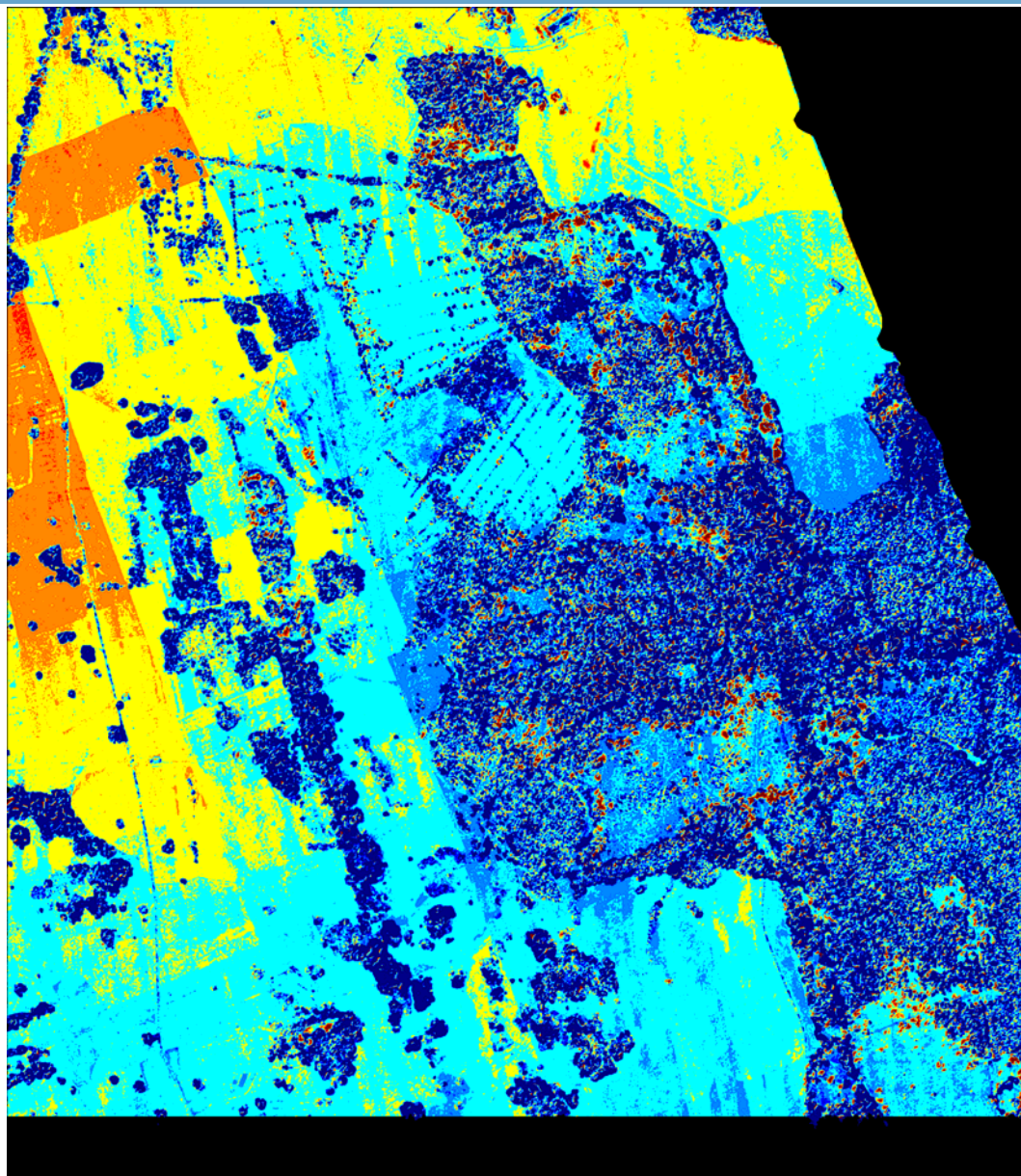
2002_DSM: template

1997_DSM: search

- **Red** areas show the deforestation!
- **Blue** areas show the growth!



Experimental results 6: Change detection, deforestation analysis



Residuals of the Euclidean distances after the LS3D matching of

2002_DSM: template

2001_LIDAR_DSM: search

- **Small Red spots** show the loss of individual trees during 1 year
- **Blue areas** show the growth, but also including the partial penetration of LIDAR
- **Orange areas** are due to image orientation differences between two flight strips

-1.5m

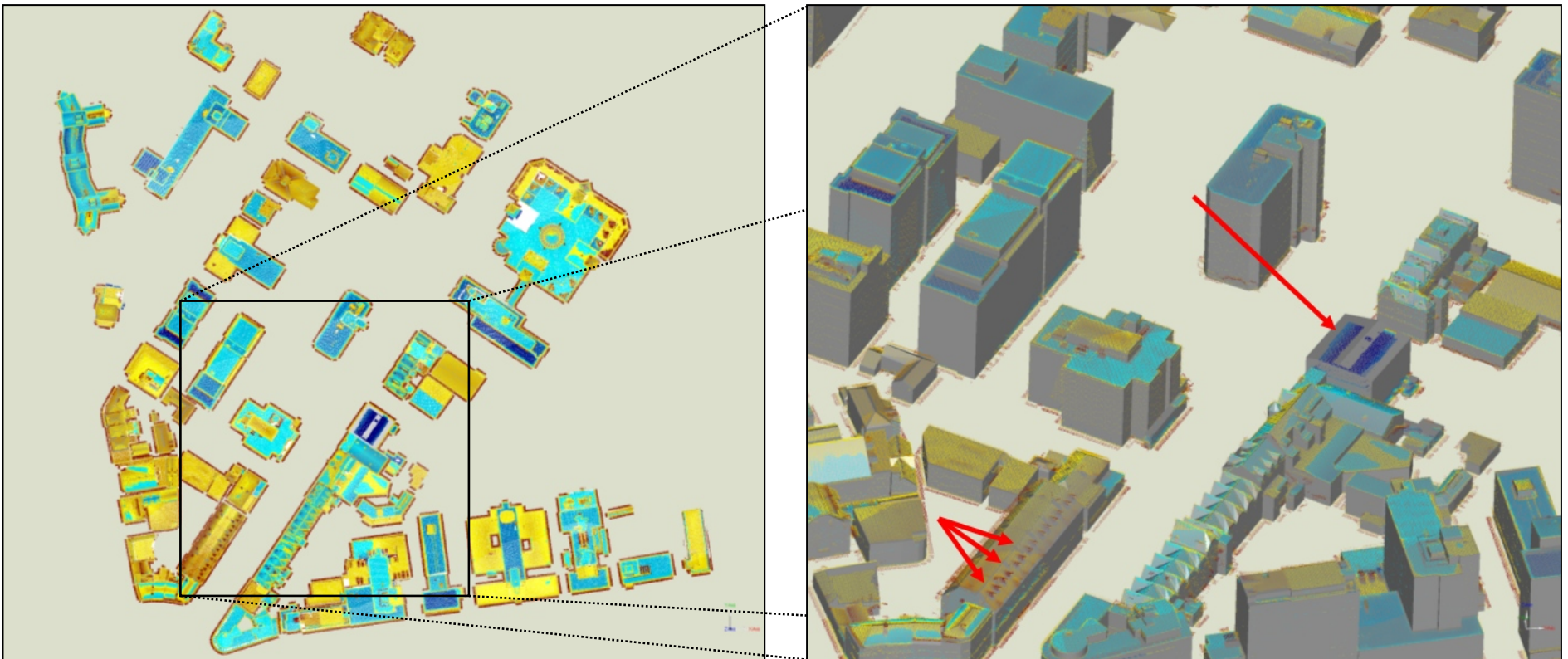
0m

1.5m

Experimental results 7: Quality assessment of 3D building data

Input data to be assessed: 3D building models given in
CyberCity Modeler (CyberCity AG, Zurich) format

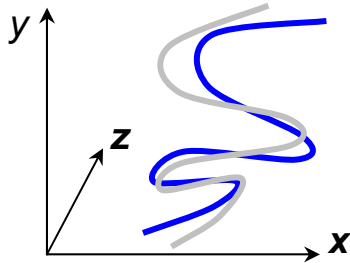
Verification (reference) data : airborne laser scanning (ALS) pointcloud data



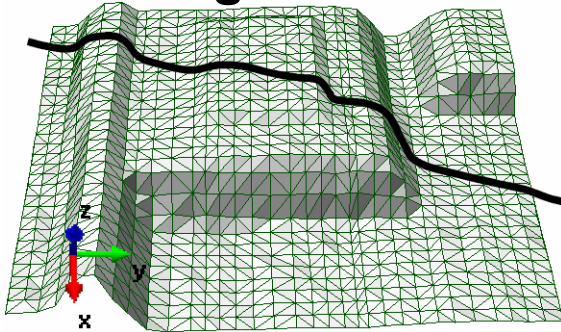
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Further Extensions #1, #2 and #3:

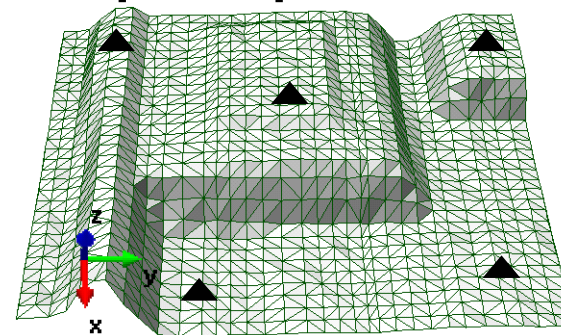
- **Least Squares 3D Curve Matching**



- **Matching of 3D curves with a 3D surface**



- **Matching of 3D sparse points with a 3D surface**



Further Extensions #4 : Objective

- **Simultaneous Co-registration and Georeferencing of Multiple pointclouds**

Objective: to develop a combined mathematical model for **simultaneous**

- co-registration
- georeferencing
- of multiple 3D surfaces

Further Extensions #4 : Mathematical model

m group of (geometric) surface (correspondence) observation equations

$$-e_1 = \mathbf{A}_1 \mathbf{x} - l_1, \mathbf{P}_1$$

$$-e_2 = \mathbf{A}_2 \mathbf{x} - l_2, \mathbf{P}_2$$

$$\vdots \quad \quad \quad \vdots$$

$$-e_m = \mathbf{A}_m \mathbf{x} - l_m, \mathbf{P}_m$$

combined under one sub-system as

$$-e = \mathbf{A} \mathbf{x} - l, \mathbf{P}$$

The parameters as stochastic quantities,

$$-e_b = \mathbf{I} \mathbf{x} - l_b, \mathbf{P}_b$$

Reference point observations are formulated as 3D similarity transformations from local pointcloud systems \rightarrow to the object coordinate system

$$-e_d = \mathbf{A}_d \mathbf{x} - l_d, \mathbf{P}_d$$

Given coordinates of the CP are not error-free quantities.

They are treated as observations with their associated weight matrices as

$$-e_e = \mathbf{A}_e \mathbf{x} - l_e, \mathbf{P}_e$$

Further Extensions #4 : Estimation Model

The hybrid system → combined adjustment type

LS solution:

$$\hat{\mathbf{x}} = \left(\mathbf{A}^T \mathbf{P} \mathbf{A} + \mathbf{P}_b + \mathbf{A}_d^T \mathbf{P}_d \mathbf{A}_d + \mathbf{A}_e^T \mathbf{P}_e \mathbf{A}_e \right)^{-1} \left(\mathbf{A}^T \mathbf{P} \mathbf{l} + \mathbf{P}_b \mathbf{l}_b + \mathbf{A}_d^T \mathbf{P}_d \mathbf{l}_d + \mathbf{A}_e^T \mathbf{P}_e \mathbf{l}_e \right)$$

Iterative solution

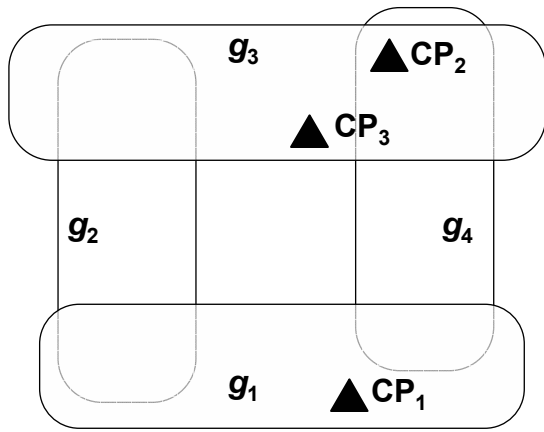
In each iteration

all surfaces → transform to a new state

re-evaluate : design matrix & discrepancies vector

Stop the iteration

Further Extensions #4 : Matrix structures



A hypothetical example:

- 4 four pointclouds
- and 3 CPs

Design matrix



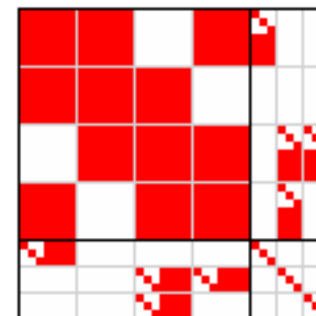
surface
geometry

parameters

georeferencing

CP coordinates

Normal matrix



Further Extensions #4 : Alfred Escher project

In cooperation with

CREDIT SUISSE



<http://www.photogrammetry.ethz.ch/research/escher/>

Further Extensions #4 : Alfred Escher project



FARO LS880 HE80

- Scanning in 2 nights
- 36 scans with 4.4 million points in the AOI
- On a cherry-picker
- Average point spacing 1 cm.

Further Extensions #4 : Alfred Escher project



Further Extensions #4 : Alfred Escher project

- Only multi-surface matching, no georeferencing
- 16 iterations with a **sigma naught of 2.7 mm.**
- 20,442,040 surface correspondences

- **18 hours processing time (fast computation under development!)**
on a laptop (Intel dual-core 2.16 GHz CPU and 2 GB memory)

- File-access oriented design of our software implementation.
Max 2 surfaces → in memory
- **Memory request < 300 MB**

Further Extensions #4 : Alfred Escher project



- Surface triangulation with Geomagic Studio
- No editing!

Further Extensions #4 : Alfred Escher project



Physical replica production (scale 1/2)

Conclusions:

- Generalization of 2D LSM => 3D surface matching,
- Estimates 3D transformation parameters, Generalized Gauss-Markoff model,
 $\min = \text{SUM}(\text{SQR}(\text{Euclidean distances}))$
- Non-linear model, need for initial approximations,

Advantages:

- **Rigorous** mathematical model
- Matching of **arbitrarily oriented 3D surfaces**, without using explicit tie points,
- Fully considers the **3D geometry**
- **Few iterations**, 5-6 typically, (ICP, 20-30-50-more),
- Provides internal **quality indicators**,
- Capability to match surfaces in **different quality and resolution**,
- **Flexible** mathematical model for further algorithmic extensions,
- **Many application** areas:
3D modeling, quality inspection, cultural heritage, accuracy analysis,
change detection, etc..

THANK YOU FOR YOUR ATTENTION!

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